

General Form of Equations of Straight Lines

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General Form of Equations of Straight Lines

Below is the general form of the equation of a straight line.



The equation of a straight line can be expressed in the form

$$Ax + By + C = 0$$

where A , B and C are constants with A and B not both zero. It is called the **general form** of the equation of a straight line.

General Form of Equations of Straight Lines

Example 1

Convert the following equations of straight lines into the general form.

(a) $3y = 7x - 2$ (b) $y = \frac{1}{4}x - 5$

(c) $y + 2 = 6(x + 1)$

(a) $3y = 7x - 2$
 $7x - 3y - 2 = 0$

(b) $y = \frac{1}{4}x - 5$
 $4y = x - 20$
 $x - 4y - 20 = 0$

(c) $y + 2 = 6(x + 1)$
 $y + 2 = 6x + 6$
 $6x - y + 4 = 0$

General Form of Equations of Straight Lines



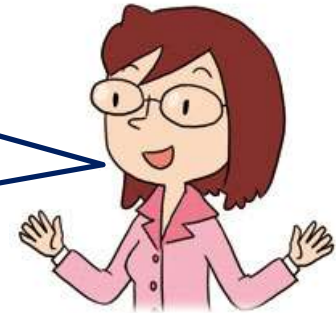
Consider the equation of a straight line L written in the general form $Ax + By + C = 0$.

Let us look at the three cases below.

| Case | Equation of L | Remark |
|--------------------------------------|--|--|
| (1) $A = 0, B \neq 0$ | $By + C = 0$, i.e. $y = -\frac{C}{B}$ | L is a horizontal line and its slope is 0. |
| (2) $B = 0, A \neq 0$ | $Ax + C = 0$, i.e. $x = -\frac{C}{A}$ | L is a vertical line and its slope is undefined. |
| (3) $C = 0, B \neq 0,$ $A \neq 0$ | $Ax + By = 0$ | L passes through the origin. |

General Form of Equations of Straight Lines

We can get the intercepts and the slope easily from the general form of the equation of a straight line.



Consider the equation of a straight line in general form:

$$Ax + By + C = 0 \dots\dots (1) \quad , \text{ where } A \neq 0 \text{ and } B \neq 0.$$

To find the x -intercept, we put $y = 0$ into (1).

$$Ax + B(0) + C = 0$$
$$x = -\frac{C}{A}$$

$$\text{The } x\text{-intercept of the straight line} = -\frac{C}{A}$$

General Form of Equations of Straight Lines

Consider the equation of a straight line in general form:

$$Ax + By + C = 0 \dots\dots (1) \quad , \text{ where } A \neq 0 \text{ and } B \neq 0.$$

To find the y -intercept, we put $x = 0$ into (1).

$$A(0) + By + C = 0$$
$$y = -\frac{C}{B}$$

$$\text{The } y\text{-intercept of the straight line} = -\frac{C}{B}$$

General Form of Equations of Straight Lines

Consider the equation of a straight line in general form:

$$Ax + By + C = 0 \dots\dots (1) \quad , \text{ where } A \neq 0 \text{ and } B \neq 0.$$

Since the straight line cuts the x -axis at $\left(-\frac{C}{A}, 0\right)$, and the y -axis at $\left(0, -\frac{C}{B}\right)$,

$$\text{The slope of the line} = \frac{-\frac{C}{B} - 0}{0 - \left(-\frac{C}{A}\right)} = -\frac{A}{B}$$

$$\text{Slope of the straight line} = -\frac{A}{B}$$

General Form of Equations of Straight Lines

Example 2

- (a) Find the slope, the x -intercept and the y -intercept of the straight line $L: 3x - 5y + 2 = 0$.
- (b) Does the point $P(1, -1)$ lie on L ?
- (c) L passes through a point $Q(h, 1)$. Find the value of h .

(a) Since $A = 3$, $B = -5$ and $C = 2$,

$$\text{slope of } L = -\frac{3}{-5} = \underline{\underline{\frac{3}{5}}}$$

$$x\text{-intercept} = \underline{\underline{-\frac{2}{3}}}$$

$$y\text{-intercept} = -\frac{2}{-5} = \underline{\underline{\frac{2}{5}}}$$

General Form of Equations of Straight Lines

Example 2

- (a) Find the slope, the x -intercept and the y -intercept of the straight line $L: 3x - 5y + 2 = 0$.
- (b) Does the point $P(1, -1)$ lie on L ?
- (c) L passes through a point $Q(h, 1)$. Find the value of h .

(b) Put $x = 1$ and $y = -1$ into $3x - 5y + 2 = 0$.

$$\text{L.H.S.} = 3(1) - 5(-1) + 2 = 10$$

$$\text{R.H.S.} = 0$$

$$\therefore \text{L.H.S.} \neq \text{R.H.S.}$$

i.e. $(1, -1)$ does not satisfy the equation $3x - 5y + 2 = 0$.

$\therefore P(1, -1)$ does not lie on L .

General Form of Equations of Straight Lines

Example 2

- (a) Find the slope, the x -intercept and the y -intercept of the straight line $L: 3x - 5y + 2 = 0$.
- (b) Does the point $P(1, -1)$ lie on L ?
- (c) L passes through a point $Q(h, 1)$. Find the value of h .

(c) Put $x = h$ and $y = 1$ into $3x - 5y + 2 = 0$.

$$3h - 5(1) + 2 = 0$$

$$3h - 3 = 0$$

$$h = \underline{1}$$